Quiz 1

 $\begin{array}{ll} \star \mbox{ Answer and mark clearly the questions in the provided answer sheets.} \\ \mbox{Write down your name and student's ID on the each answer sheet you used.} \\ \star \mbox{ Note: No points will be given if no arguments are provided for an answer.} \\ \mbox{ Good Luck!} & \sim \sim Yuling \\ \end{array}$ 

1. (10 points) Find the domain and range of the function

$$f(x) = \frac{x}{\sqrt{x-9}}$$

- 2. (10 points) Determine whether the function  $f(x) = x^4$  is one-to-one. If it is, find its inverse function.
- 3. (10 points) Find the inverse function of f, where  $f(x) = \sqrt{x^2 4}, x \ge 2$ .
- 4. (50 points) Find the indicated limit or show it does not exist. If the limiting value is infinite, indicate whether it is  $\infty$  or  $-\infty$ .

(a) 
$$\lim_{x \to -1} \frac{2x^2 - x - 3}{x + 1}$$
, (b)  $\lim_{\Delta t \to 0} \frac{(t + \Delta t)^2 - 4(t + \Delta t) + 2 - (t^2 - 4t + 2)}{\Delta t}$ ,  
(c)  $\lim_{x \to 3} \frac{\sqrt{x + 1} - 2}{x - 3}$ , (d)  $\lim_{x \to 0} \frac{\sqrt{x + 2} - \sqrt{2}}{x}$ , (e)  $\lim_{x \to 0^-} \frac{x + 1}{x}$ 

5. (10 points) Discuss the continuity of the function

$$f(x) = \frac{x - 1}{x^2 - 4x + 3}$$

on the closed interval [0, 4]. If there are any discontinuities, determine whether they are removable.

6. (10 points) Find the constants a and b such that the function f(x) is continuous on the entire real number line, where

$$f(x) = \begin{cases} 2 & x \le -1 \\ ax + b & -1 < x < 3 \\ -2 & x \ge 3 \end{cases}$$