

★ Answer and mark clearly the questions in the provided answer sheets.
Write down your name and student's ID on the each answer sheet you used.
* **Note:** No points will be given if no arguments are provided for an answer.

For your information:

- $\int \sin u \, du = -\cos u + C$
- $\int \cos u \, du = \sin u + C$
- $\int \sec^2 u \, du = \tan u + C$
- $\int \sec u \tan u \, du = \sec u + C$
- $\sin^2 u + \cos^2 u = 1$ and $\tan^2 u + 1 = \sec^2 u$

Good Luck!

~~ Yes ☺

1. (60 points) Find

(a) $\int \frac{x^2 + 3}{(x^3 + 9x - 4)^2} dx$

(b) $\int \frac{x^2 + 2x + 5}{x - 1} dx$

(c) $\int \frac{1}{x \ln x} dx$

(d) $\int \frac{1 + e^{-x}}{1 + xe^{-x}} dx$

(e) $\int \frac{e^{2x} + 2e^x + 1}{e^x} dx$

(f) $\int x(\ln x)^2 dx$

2. (10 points) Find $f(x)$ whose graph passes through the point $(4, 6)$, and

$$f'(x) = \frac{e^{2/x}}{x^2}.$$

3. (10 points) Find a function f that satisfies the differential equation and the initial conditions: $f''(x) = 2$, $f'(2) = 5$, $f(2) = 10$.

4. (20 points) Find

(a) $\int \frac{\sin x}{1 + \cos x} dx$

(b) $\int \sec^6 \frac{x}{4} \tan \frac{x}{4} dx$