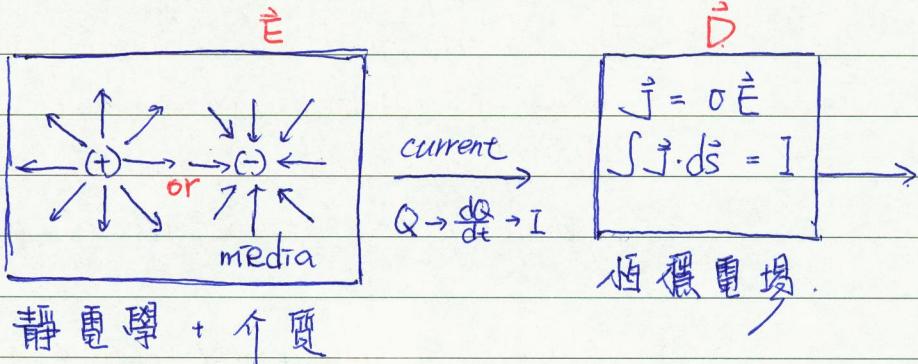


## Chapter 1-4.



## Chapter 5.

moving electron

A. Divergency

B. curl  $\nabla \times \vec{E} = 0$



$$\frac{\vec{E} \cdot \Delta A}{\Delta V} = \text{Density.}$$

$$\oint \vec{E} \cdot d\vec{s} = \int P dv$$

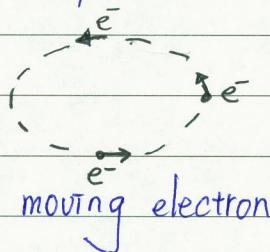


$$\int \vec{E} \cdot d\vec{l} \Rightarrow \oint q \vec{E} \cdot d\vec{l} = 0$$

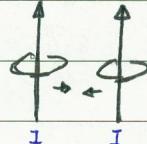
potential closed path.

## Chapter 5.

Ampere in 1820s experiment.



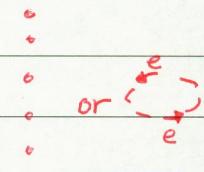
Case I:



Case II:



or  $+q$ , find.



moving.

- \* The definition of magnetic field is slightly more difficult or formula.

The electric field at a given point in space is defined in terms of the force the electric field exerts on a small stationary test charge placed there.

- \* Magnetic forces only acting on moving charges, so it is natural to use the magnetic force  $\vec{F}$  exerts on a positive charge  $q$ , where velocity is  $\vec{v}$ .

So Ampere can write down as  
$$\vec{F} \propto q(\vec{v} \times \vec{B}) = qvB \sin\theta$$

- \* The magnitude is specified by

$$B = \frac{F}{qv \cdot \sin\theta}$$

The unit of magnetic field in SI is

$$\frac{\text{Newtons}}{\text{Ampere} \cdot \text{meter}} = \text{tesla (T)}$$

- \* Thus a charged particle  $q$  of momentum  $\vec{p}$  has the classical equation of motion.

$$\vec{F} = ma \Rightarrow \frac{d\vec{P}}{dt} = \frac{d(m\vec{v})}{dt} = q(\vec{E} + \vec{v} \times \vec{B})$$

+ It is interesting to note that the magnetic field DOES NOT mechanical work on a moving charged particle.

\* Newton said  $\vec{F} \cdot d\vec{l} = dW = F dl \cos\theta$   
 $\cos\theta = 1 \Rightarrow F dl$

\* Prove the mechanical work is zero.

(1) The vector product  $\vec{v} \times \vec{B}$  is the force incorporate the fact that the force due to the  $\vec{B}$ -field is perpendicular both  $\vec{B}$  &  $\vec{v} \Rightarrow \vec{B} \cdot (\vec{v} \times \vec{B}) = 0$

(2) or  $\vec{F} = \frac{d\vec{P}}{dt} \Rightarrow dW_{mag} = \vec{F} \cdot d\vec{l} = q(\vec{v} \times \vec{B}) \cdot \vec{v} dt$   
 $= q d\theta [(\vec{v} \times \vec{B}) \cdot \vec{v}] = 0$