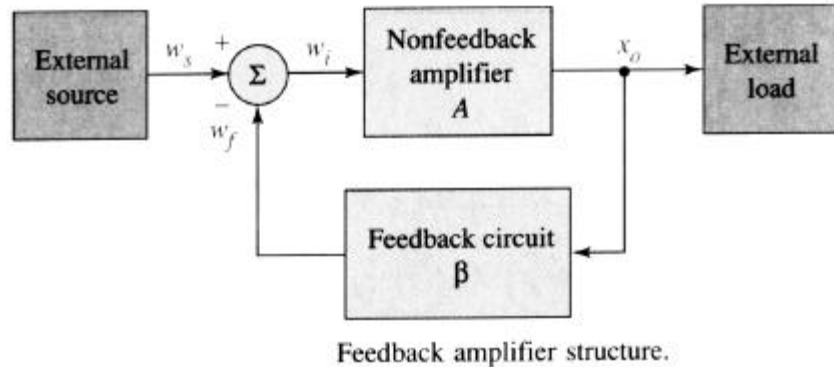


回授概論

Introduction of Feedback Circuits

General Scheme of a feedback circuit



輸出訊號 x_o 及訊號 $w_{s,i,f}$ 可為電流或電壓訊號

$$x_o = Aw_i = A(w_s - w_f) = A(w_s - bx_o)$$

$$A_f = \frac{x_o}{w_s} = \frac{A}{1 + Ab}$$

$$\text{回授訊號為 } w_f = bx_o = \frac{Ab}{1 + Ab} w_s$$

一般使用時, $Ab > 0$, 稱為負回授。若 $Ab = -1$, 則電路開始振盪。

負回授對放大器的影響

1. 放大率減小。
2. 降低放大率對電路元件參數的靈敏度。

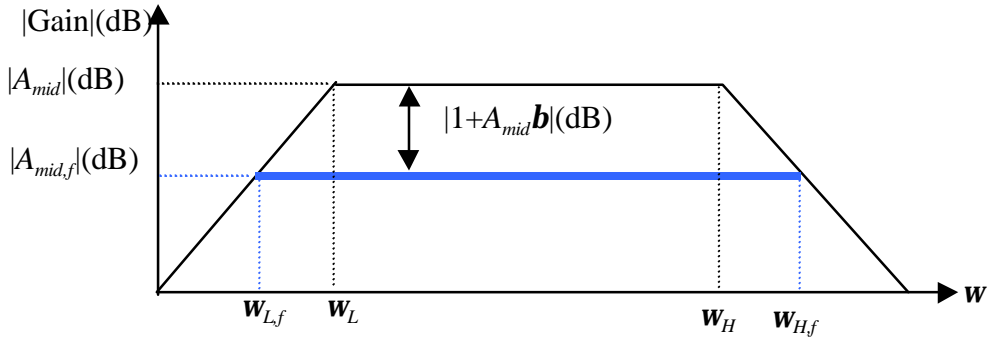
$$S_p^{A_f} = \frac{1}{1 + Ab} S_p^A$$

直接由靈敏度定義即可證明。

3. 增加頻寬。

$$w_H \rightarrow (1 + Ab)w_H$$

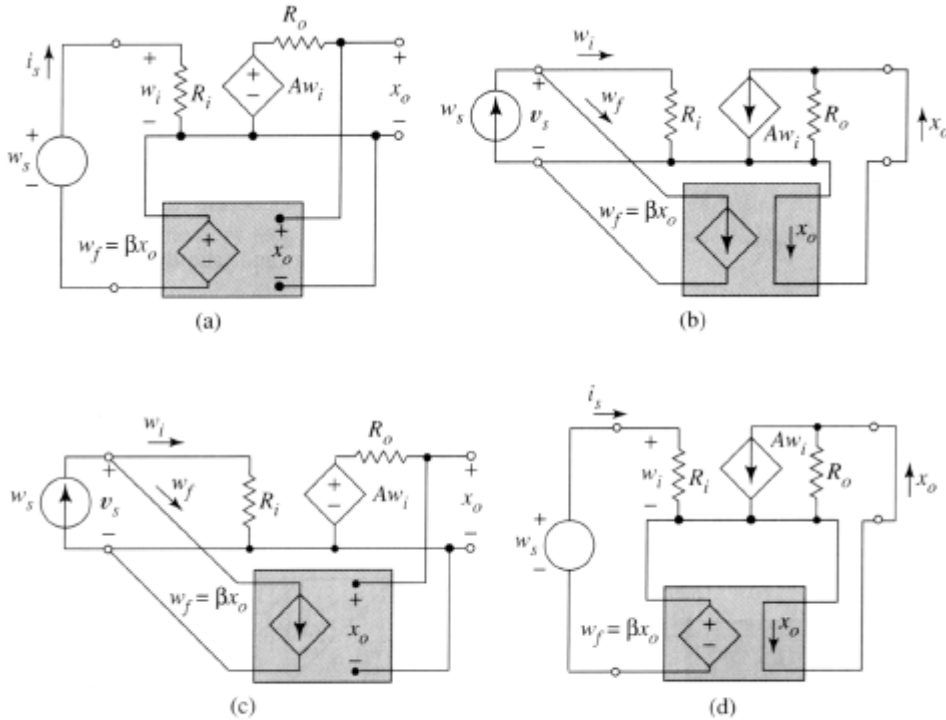
$$w_L \rightarrow \frac{w_L}{(1 + Ab)}$$



4. 減小放大器之非線性失真。

由於放大器的非線性失真在負回授時減掉，或說真正的輸入訊號 w_i 變小。

5. 改善輸入及輸出阻抗。



Feedback strategies for different design goals: (a) voltage-series feedback for a voltage amplifier; (b) current-shunt feedback for a current amplifier; (c) voltage-shunt feedback for a transresistance amplifier; (d) current-series feedback for a transconductance amplifier.

Feedback Amplifier Classifications

Design Goal	Feedback Class	Input Resistance	Output Resistance	Ideal Source	Ideal Load	β Circuit Two-Port Model
Voltage amplifier (VCVS)	Voltage series	Increases	Decreases	Voltage	Open circuit	h
Transresistance amplifier (CCVS)	Voltage shunt	Decreases	Decreases	Current	Open circuit	y
Current amplifier (CCCS)	Current shunt	Decreases	Increases	Current	Short circuit	g
Transconductance amplifier (VCCS)	Current series	Increases	Increases	Voltage	Short circuit	z

Voltage-Series Feedback

計算輸入阻抗

$$w_s = i_s R_i + \mathbf{b}[A(i_s R_i)]$$

$$R_{i,f} = \frac{w_s}{i_s} = R_i(1 + \mathbf{A}\mathbf{b}) \quad \text{不考慮輸出負載}$$

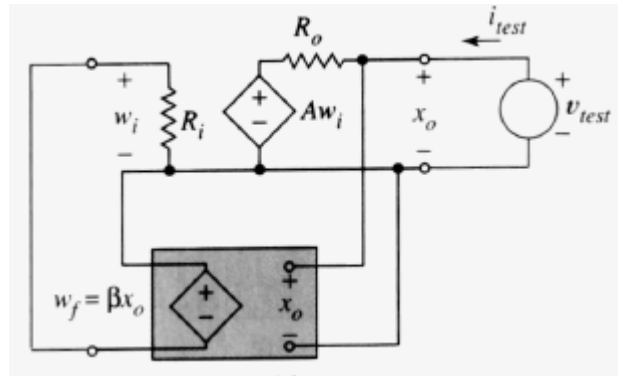
計算輸出阻抗

$$w_i = -\mathbf{b}u_{test}$$

$$\begin{aligned} \mathbf{u}_{test} &= R_o i_{test} + \mathbf{A}w_i \\ &= R_o i_{test} - \mathbf{A}\mathbf{b}u_{test} \end{aligned}$$

$$R_{of} = \frac{\mathbf{u}_{test}}{i_{test}}$$

$$= \frac{R_o}{1 + \mathbf{A}\mathbf{b}}$$



Current-Shunt Feedback

計算輸入阻抗

$$w_s = \frac{\mathbf{u}_s}{R_i} + \mathbf{b}[A(\frac{\mathbf{u}_s}{R_i})]$$

$$R_{i,f} = \frac{\mathbf{u}_s}{w_s} = \frac{R_i}{(1 + \mathbf{A}\mathbf{b})} \quad \text{不考慮輸出負載}$$

計算輸出阻抗

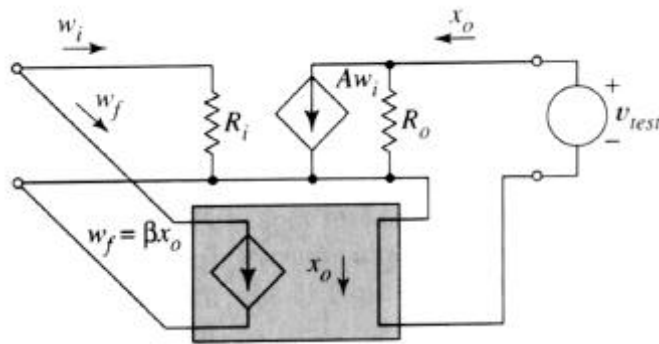
$$w_i = -\mathbf{b}x_o$$

$$x_o = \frac{\mathbf{u}_{test}}{R_o} + Aw_i$$

$$= \frac{\mathbf{u}_{test}}{R_o} - A\mathbf{b}x_o$$

$$R_{of} = \frac{\mathbf{u}_{test}}{x_o}$$

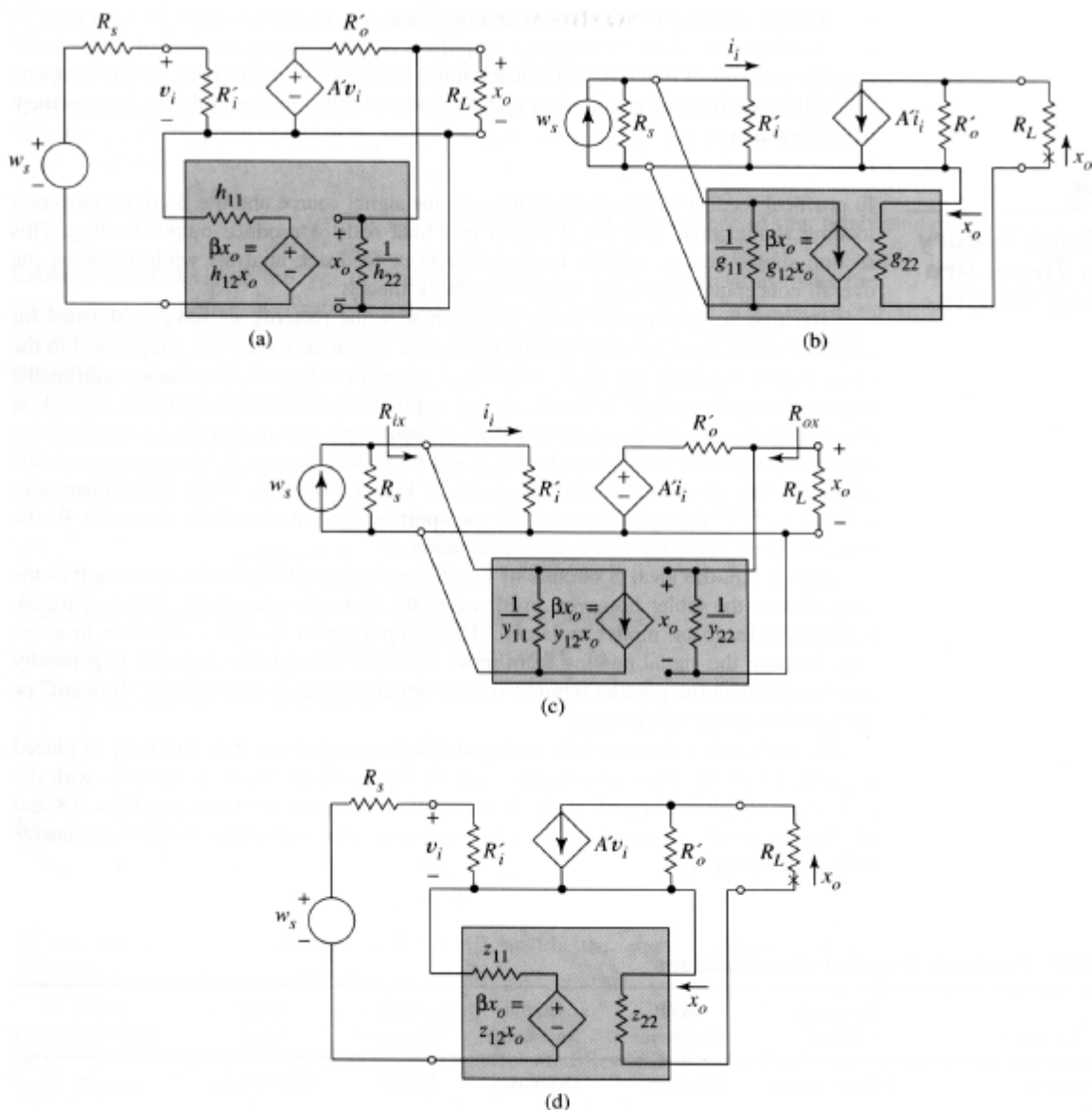
$$= R_o(1 + A\mathbf{b})$$



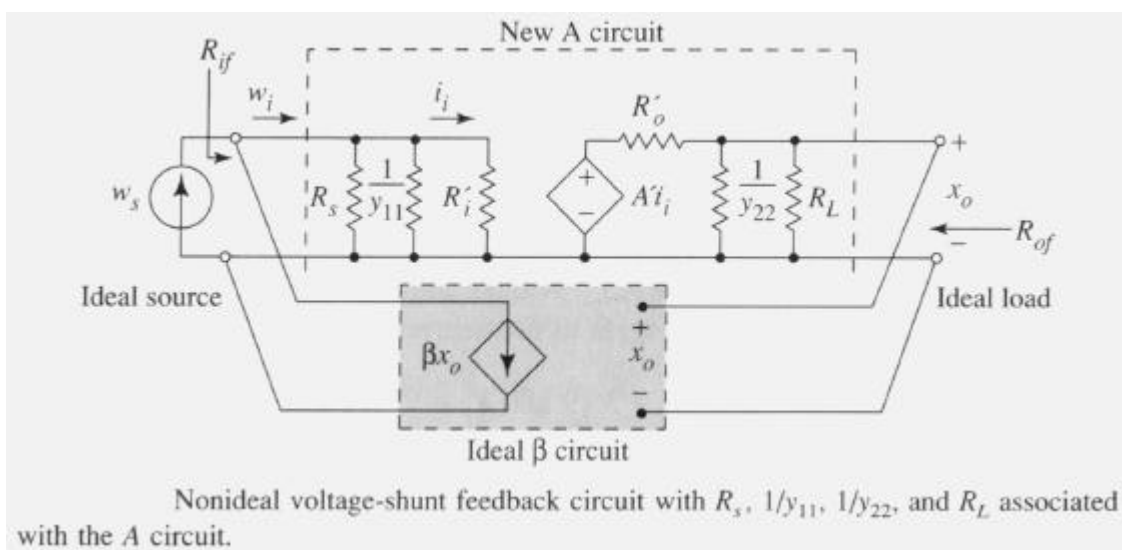
考慮回授電路的負載效應

當回授電路(β network)不是理想的 dependent source 時，他的負載效應必須考慮。處理的方法是將回授電路的輸入及輸出阻抗和主要放大電路合併，回授電路則只剩下理想的 dependent source。分析時則先分析包括回授電路的輸入及輸出阻抗但無回授($\mathbf{b}=0$)的電路，再考慮回授的影響。

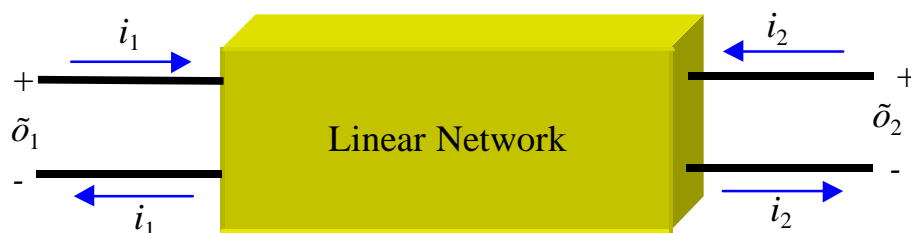
在分析電路之前，回授電路部分必須先找出來，並以線性雙埠模型 (linear two-port model) 表示，而且以單向(unilateral)電路來做近似，即放大器的輸出訊號可經由回授電路回到輸入，但輸入訊號則無法由回授電路到輸出。



Nonideal feedback circuits: (a) voltage series; (b) current shunt; (c) voltage shunt; (d) current series.



線性雙埠模型 (linear two-port model)



$$\begin{pmatrix} \mathbf{u}_1 \\ \mathbf{u}_2 \end{pmatrix} = \begin{pmatrix} z_{11} & z_{12} \\ z_{21} & z_{22} \end{pmatrix} \begin{pmatrix} i_1 \\ i_2 \end{pmatrix} \quad \text{z Parameters}$$

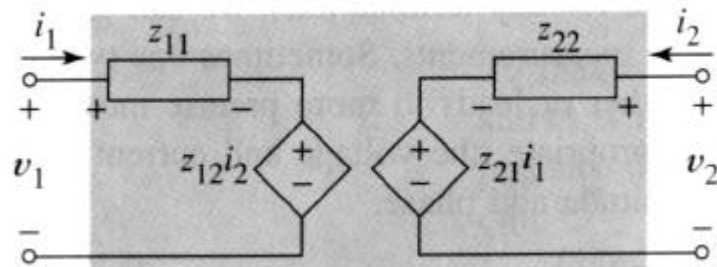
$$\begin{pmatrix} i_1 \\ i_2 \end{pmatrix} = \begin{pmatrix} y_{11} & y_{12} \\ y_{21} & y_{22} \end{pmatrix} \begin{pmatrix} \mathbf{u}_1 \\ \mathbf{u}_2 \end{pmatrix} \quad \text{y Parameters}$$

$$\begin{pmatrix} \mathbf{u}_1 \\ i_2 \end{pmatrix} = \begin{pmatrix} h_{11} & h_{12} \\ h_{21} & h_{22} \end{pmatrix} \begin{pmatrix} i_1 \\ \mathbf{u}_2 \end{pmatrix} \quad \text{h Parameters}$$

$$\begin{pmatrix} i_1 \\ \mathbf{u}_2 \end{pmatrix} = \begin{pmatrix} g_{11} & g_{12} \\ g_{21} & g_{22} \end{pmatrix} \begin{pmatrix} \mathbf{u}_1 \\ i_2 \end{pmatrix} \quad \text{g Parameters}$$

等效電路

z Parameters

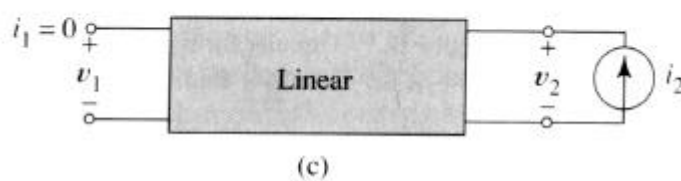
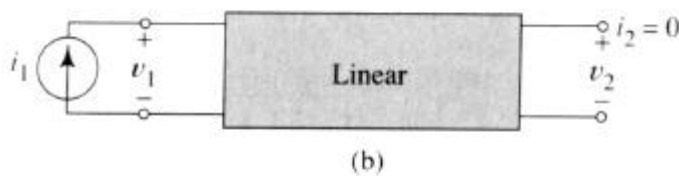
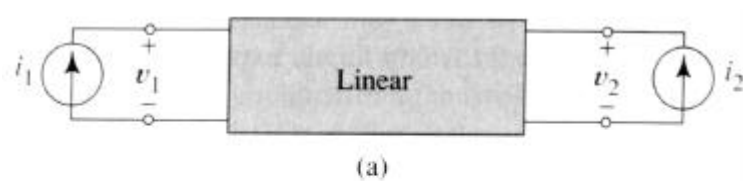


$$z_{11} = \frac{\mathbf{u}_1}{i_1} \Big|_{i_2 = 0} \quad \text{open-circuit input impedance}$$

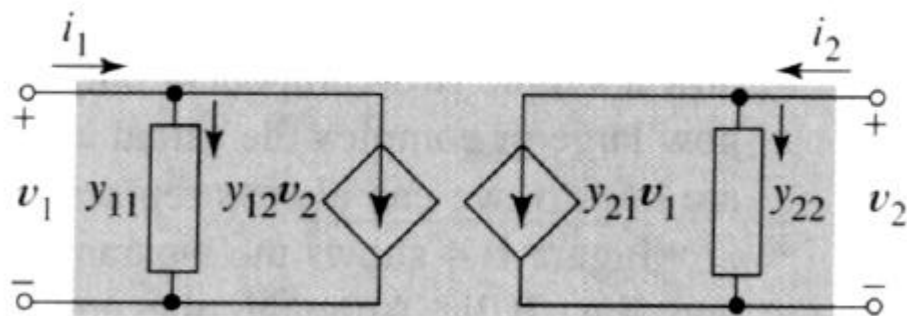
$$z_{21} = \frac{\mathbf{u}_2}{i_1} \Big|_{i_2 = 0} \quad \text{open-circuit forward transfer impedance}$$

$$z_{12} = \frac{\mathbf{u}_1}{i_2} \Big|_{i_1 = 0} \quad \text{open-circuit reverse transfer impedance}$$

$$z_{22} = \frac{\mathbf{u}_2}{i_2} \Big|_{i_1 = 0} \quad \text{open-circuit output impedance}$$



y Parameters

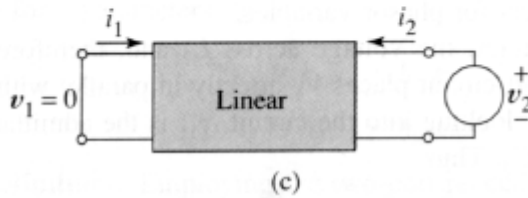
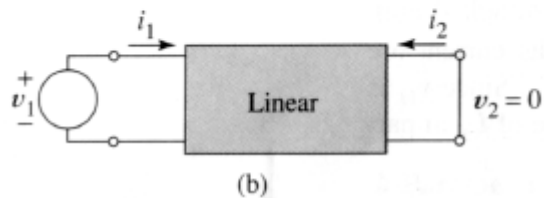
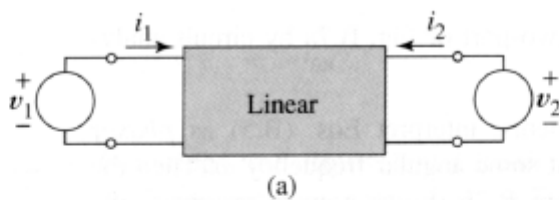


$$y_{11} = \left. \frac{i_1}{u_1} \right|_{u_2 = 0} \quad \text{short-circuit input admittance}$$

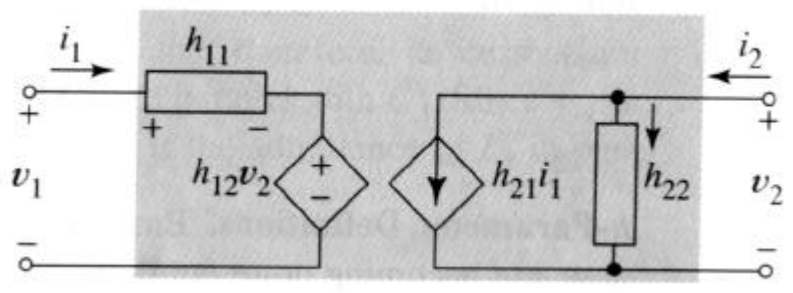
$$y_{21} = \left. \frac{i_2}{u_1} \right|_{u_2 = 0} \quad \text{short-circuit forward transfer admittance}$$

$$y_{12} = \left. \frac{i_1}{u_2} \right|_{u_1 = 0} \quad \text{short-circuit reverse transfer admittance}$$

$$y_{22} = \left. \frac{i_2}{u_2} \right|_{u_1 = 0} \quad \text{short-circuit output admittance}$$



h Parameters

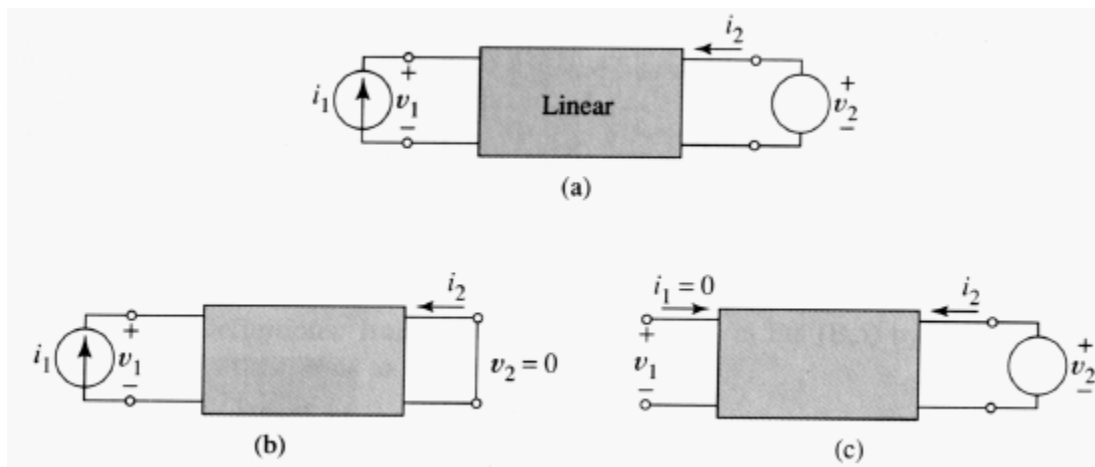


$$h_{11} = \frac{u_1}{i_1} \Big|_{u_2 = 0} \quad \text{short-circuit input impedance}$$

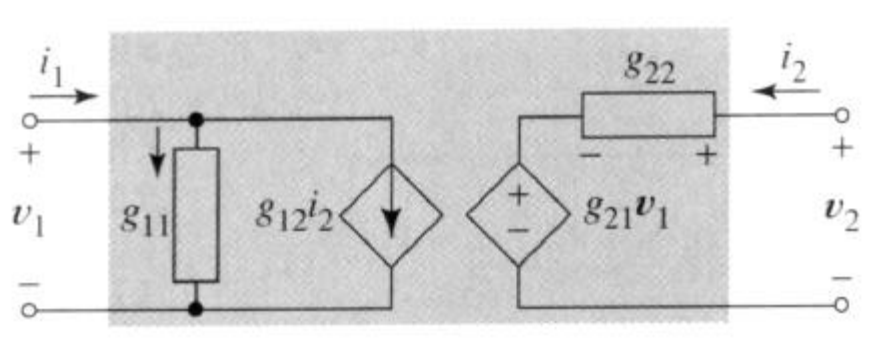
$$h_{21} = \frac{i_2}{i_1} \Big|_{u_2 = 0} \quad \text{short-circuit forward current gain}$$

$$h_{12} = \frac{u_1}{u_2} \Big|_{i_1 = 0} \quad \text{open-circuit reverse voltage gain}$$

$$h_{22} = \frac{u_1}{u_2} \Big|_{i_1 = 0} \quad \text{open-circuit output admittance}$$



g Parameters

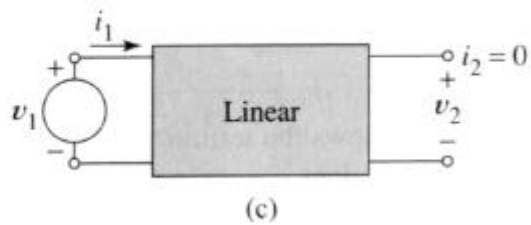
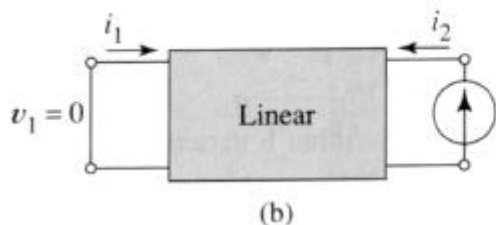
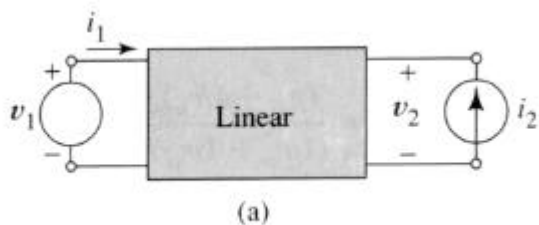


$$g_{11} = \frac{i_1}{u_1} \Big|_{i_2 = 0} \quad \text{open-circuit input admittance}$$

$$g_{21} = \frac{u_2}{u_1} \Big|_{i_2 = 0} \quad \text{open-circuit forward voltage gain}$$

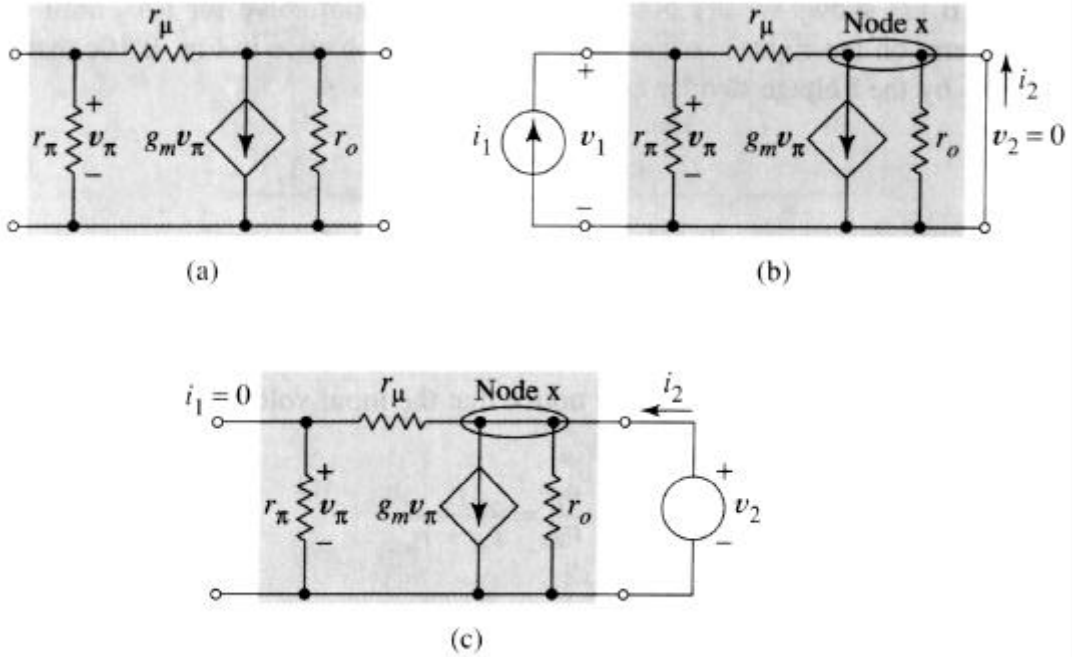
$$g_{12} = \frac{i_1}{i_2} \Big|_{u_1 = 0} \quad \text{short-circuit reverse current gain}$$

$$g_{22} = \frac{u_2}{i_2} \Big|_{u_1 = 0} \quad \text{short-circuit output impedance}$$



雙埠等效電路之實例

(1)BJT 的 h parameters



計算 h_{11} 及 h_{21} : 將輸出短路

$$h_{11} = \frac{u_1}{i_1} = r_p // r_m \equiv h_{ie}$$

if we consider the base spreading resistance.

$$[= r_b + (r_p // r_m)]$$

$$i_2 = g_m u_1 - \frac{u_1}{r_m} = \left(g_m - \frac{1}{r_m} \right) (r_p // r_m) i_1 = \left(g_m - \frac{1}{r_m} \right) h_{ie} i_1$$

$$h_{21} = \frac{i_2}{i_1} = \left(g_m - \frac{1}{r_m} \right) h_{ie} = \left(g_m - \frac{1}{r_m} \right) (r_p // r_m) = \frac{g_m - 1/r_m}{1/r_p + 1/r_m}$$

$$\equiv h_{fe}$$

計算 h_{12} 及 h_{22} : 將輸入開路

$$\mathbf{u}_p = \frac{r_p}{r_p + r_m} \mathbf{u}_2$$

$$i_2 = \frac{\mathbf{u}_2}{r_o} + g_m \mathbf{u}_p + \frac{\mathbf{u}_2}{r_p + r_m} = \left(\frac{1}{r_o} + \frac{g_m r_p}{r_p + r_m} + \frac{1}{r_p + r_m} \right) \mathbf{u}_2$$

$$h_{22} = \frac{i_2}{\mathbf{u}_2} = \frac{1}{r_o} + \frac{1 + g_m r_p}{r_p + r_m} = \frac{1}{r_o} + \frac{1 + \mathbf{b}}{r_p + r_m} \equiv h_{oe}$$

$$h_{12} = \frac{\mathbf{u}_1}{\mathbf{u}_2} = \frac{r_p}{r_p + r_m} \equiv h_{re}$$

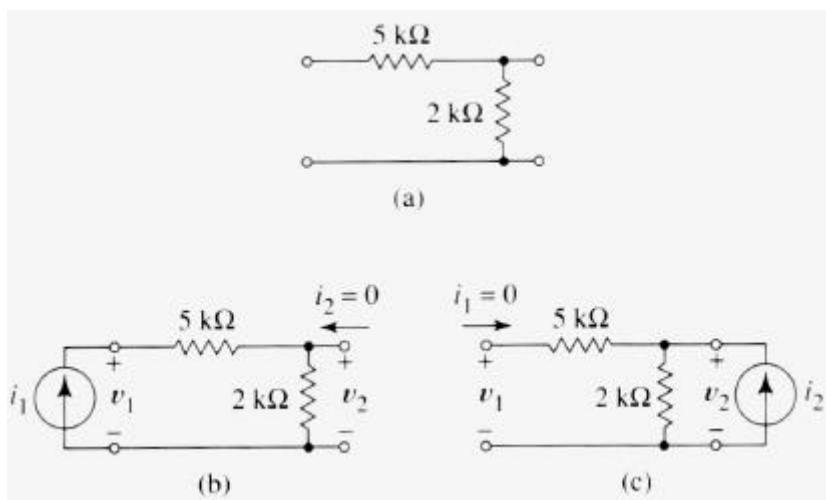
Static h Parameters for Common-Emitter BJT

h Parameter	h Parameter in Terms of Hybrid Pi Parameters	Approximate Expression for h Parameter
h_{ie}	$r_b + (r_\pi \parallel r_\mu)$	$r_b + r_\pi$
h_{fe}	$\frac{r_\mu g_m r_\pi - r_\pi}{r_\mu + r_\pi}$	β
h_{re}	$\frac{r_\pi}{r_\pi + r_\mu}$	$\frac{r_\pi}{r_\mu}$
h_{oe}	$\frac{1}{r_o} + \frac{\beta + 1}{r_\pi + r_\mu}$	$\frac{1}{r_o} + \frac{\beta}{r_\mu}$

BJT 廠商提供的數據都是 h parameters , 以及 f_t 和 C_m (或稱 C_{ob} 、 C_{cb} 、 C_c 、 C_{CBO}) , 分析前可先換為 hybrid- π model 的參數 :

1. $g_m = \frac{I_C}{V_T}$
2. $r_p = \frac{h_{fe}}{g_m}$
3. $r_b = h_{ie} - r_p$
4. $r_m = \frac{r_p}{h_{re}}$
5. $r_o = \frac{r_m}{r_m h_{oe} - h_{fe}}$
6. $C_p = \frac{g_m}{2\pi f_t} - C_m$

(2) 電阻分壓電路之 z parameters



計算 z_{11} 及 z_{21} : 將輸出開路，輸入加一電流源。

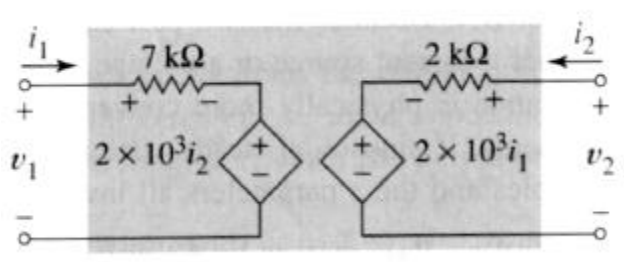
$$z_{11} = \frac{u_1}{i_1} = (5 + 2) \text{ k}\Omega = 7 \text{ k}\Omega$$

$$z_{21} = \frac{u_2}{i_1} = 2 \text{ k}\Omega = 2 \times 10^3 \text{ V/A}$$

計算 z_{22} 及 z_{12} : 將輸入開路，輸出加一電流源。

$$z_{22} = \frac{u_2}{i_2} = 2 \text{ k}\Omega$$

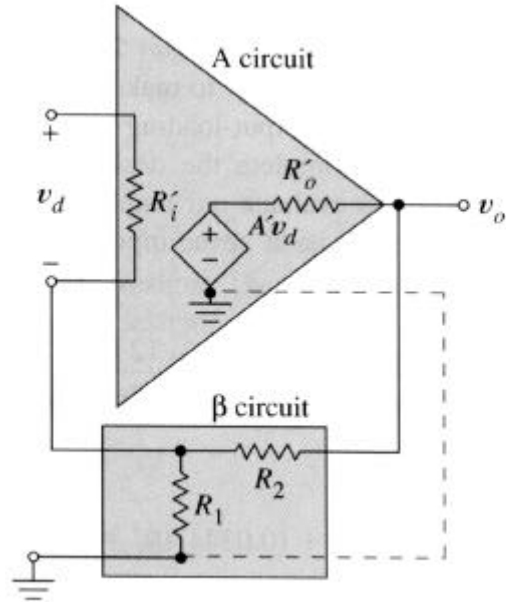
$$z_{12} = \frac{u_1}{i_2} = 2 \text{ k}\Omega = 2 \times 10^3 \text{ V/A}$$



回授差動放大器

Difference amplifier topology---voltage-series feedback

簡單的例子：



Noninverting amplifier as a feedback circuit.

右圖為一實際的電路，

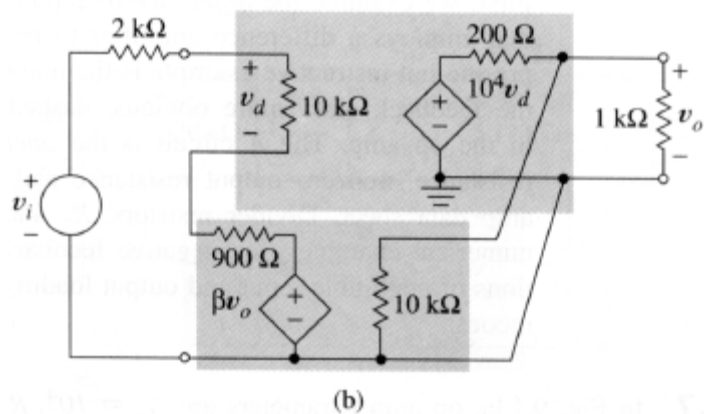
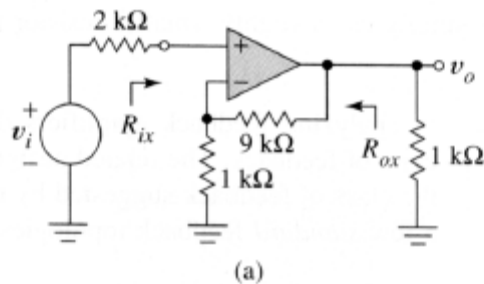
先求回授網路的

h parameters

$$h_{11} = 1 // 9 \text{ k}\Omega = 900 \Omega$$

$$h_{22} = 1 / [(1 + 9) \text{ k}\Omega] = 1 / [10 \text{ k}\Omega]$$

$$h_{12} = \mathbf{b} = 1 / (1 + 9) = 0.1$$



$h_{21} = 0.1$ (short-circuit current gain) 由於是 voltage feedback，輸入阻抗大大地增加，也就是輸入電流變得很小， $h_{12}i_{in}$ 對輸出電路影響很小，故 h_{12} 對應的 CCCS 忽略。

將回授關掉---令 $b=0$, 求包含回授電路負載效應的放大器參數 (開路參數)

$$R_i = (2 + 10 + 0.9) \text{ k}\Omega = 12.9 \text{ k}\Omega$$

$$R_o = (1 // 10 // 0.2) \text{ k}\Omega = 164 \Omega$$

$$A = \frac{u_o}{u_i} = \frac{10 \text{ k}}{10 \text{ k} + 2 \text{ k} + 900} 10^4 \frac{(1 // 10) \text{ k}}{(1 // 10) \text{ k} + 200} = 6354$$

改善因子(improving factor) $1 + bA = 1 + 6354 \times 0.1 = 636$

$$A_f = \frac{A}{1 + bA} = \frac{6354}{636} = 9.99 \approx \frac{1}{b}$$

$$R_{if} = 12.9 \times 636 \text{ k}\Omega = 8.2 \text{ M}\Omega$$

$$R_{of} = 164 / 636 \Omega = 0.258 \Omega$$

一個更實際的電路設計

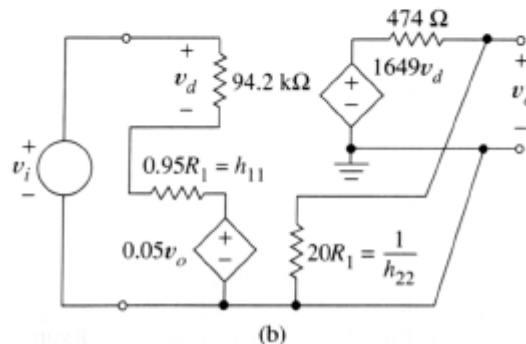
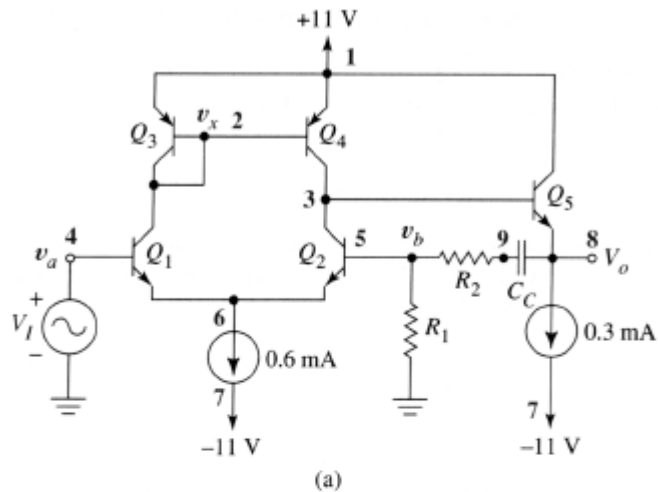
先將 R_1, R_2 移去計算無回授電路的特性 , 計算時 b 端接地。

如果我們想設計一個增益

為 20 的電壓放大器 , 即

$$A_f = 20 \approx \frac{1}{b} = \frac{1}{h_{12}}$$

$$= \frac{R_1 + R_2}{R_1}$$



$$R_2 = 19R_1$$

$$h_{11} = R_1 // R_2 = 0.95R_1$$

$$1/h_{22} = R_1 + R_2 = 20R_1$$

為避免輸入及輸出之負載效應，選擇

$$h_{11} = 0.95R_1 \ll 94.2 \text{ k}\Omega$$

$$1/h_{22} = 20R_1 \gg 474 \Omega$$

取 $R_1=270 \Omega$, $R_2=5.1 \text{ k}\Omega$ 。

將回授關掉---令 $b=0$ ，求包含回授電路負載效應的放大器參數（開路參數）。

$$R_i = 94.2 \text{ k} + 0.95 \times 270 = 94.5 \text{ k}$$

$$R_o = 474 // (20 \times 270) = 436 \Omega$$

$$A = \frac{u_o}{u_i} = \frac{94.2 \text{ k}}{94.2 \text{ k} + 0.95 \times 270} 1649 \frac{20 \times 270}{20 \times 270 + 474} = 1512$$

$$1 + bA = 1 + 1512 \times 0.0503 = 77.1$$

$$R_{if} = 94.5 \times 77.1 \text{ k}\Omega = 7.29 \text{ M}\Omega$$

$$R_{of} = 436 / 77.1 \Omega = 5.66 \Omega$$

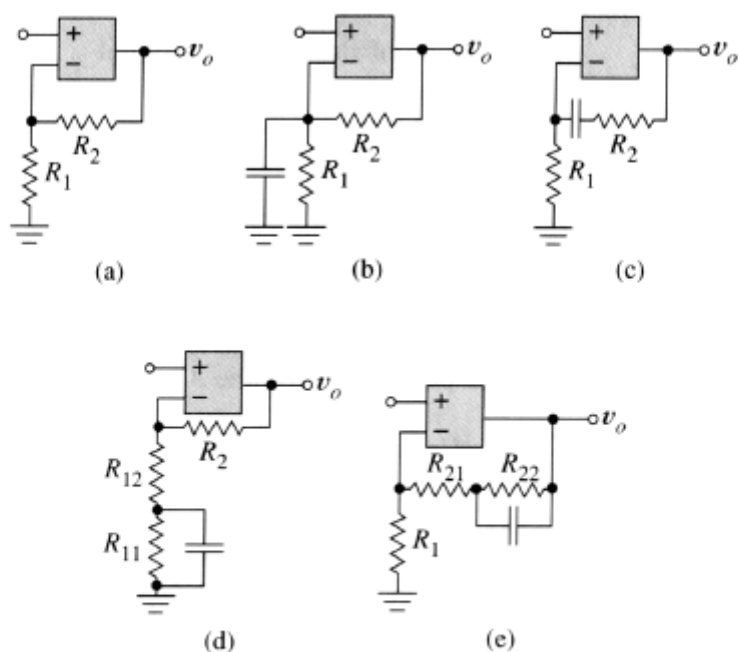
$$A_f = \frac{A}{1 + Ab} = 19.6$$

C_C 決定回授的低頻截止頻率。

注意，這樣的接法，直流無回授，直流增益遠大於交流增益，必須

注意直流偏壓的穩定性。

dc, ac, and mixed feedback

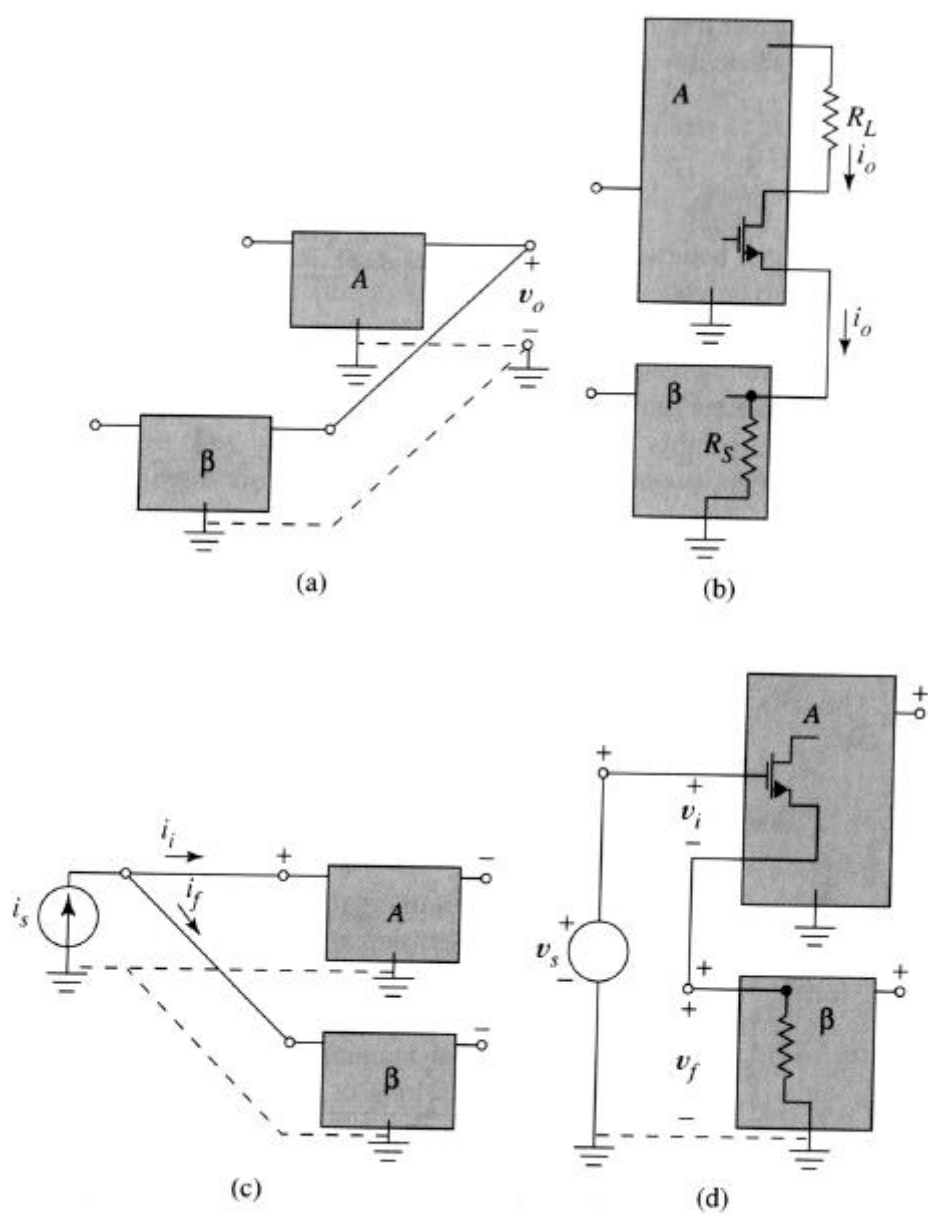


Combinations of dc and ac feedback: (a) dc and ac feedback in equal amounts; (b) dc but no ac feedback; (c) ac but no dc feedback; (d) dc feedback greater than ac feedback; (e) ac feedback greater than dc feedback.

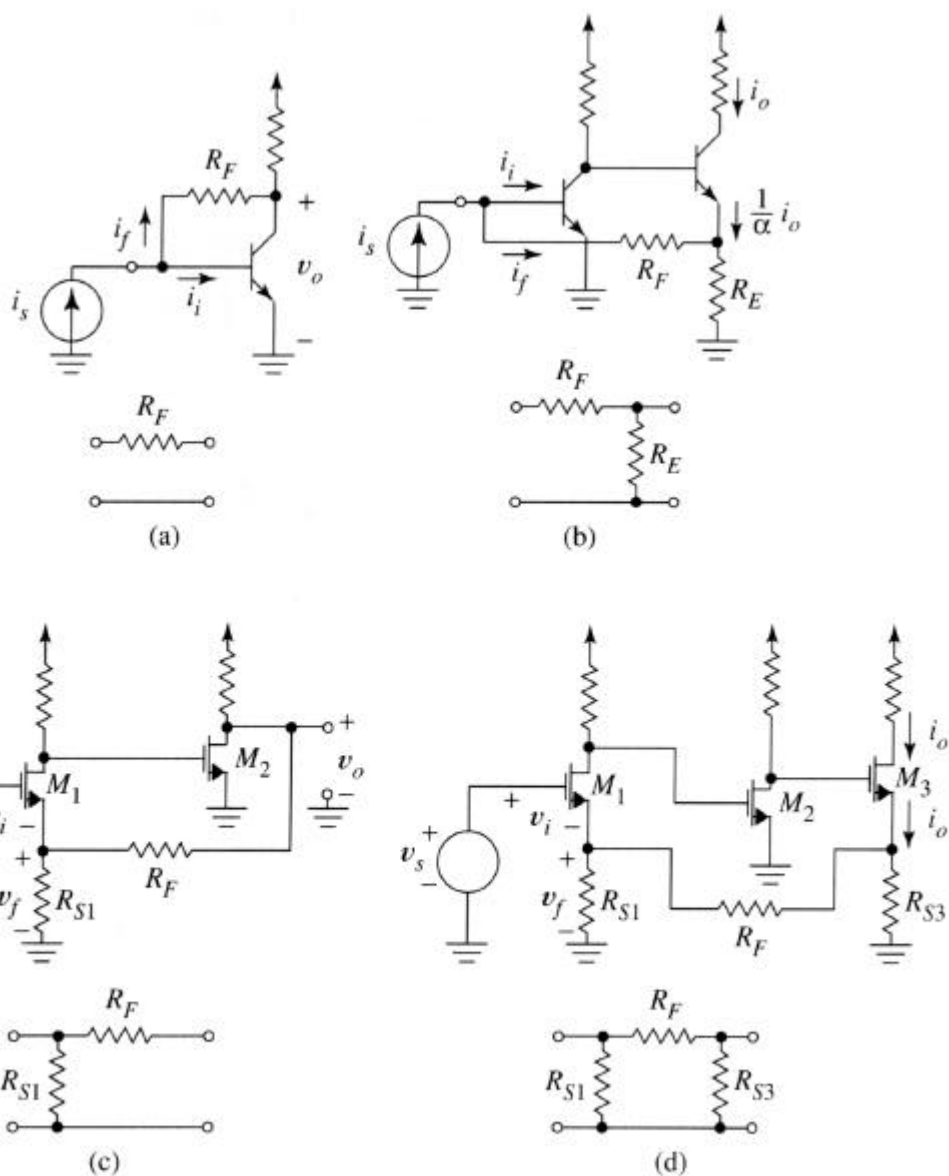
單端放大器的回授

分析最重要的(也是最困難的)步驟是判定回授的種類。

判斷的依據包括：(1)回授訊號的來源，(2)回授訊號的目的地，(3)相位(必須是負回授)。

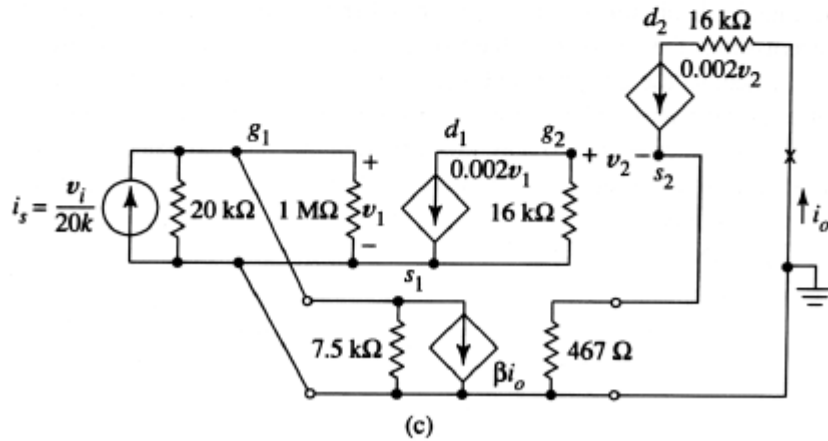
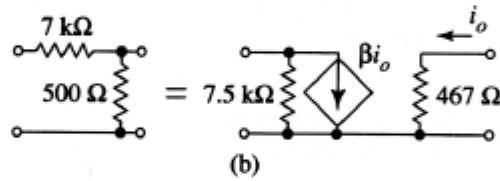
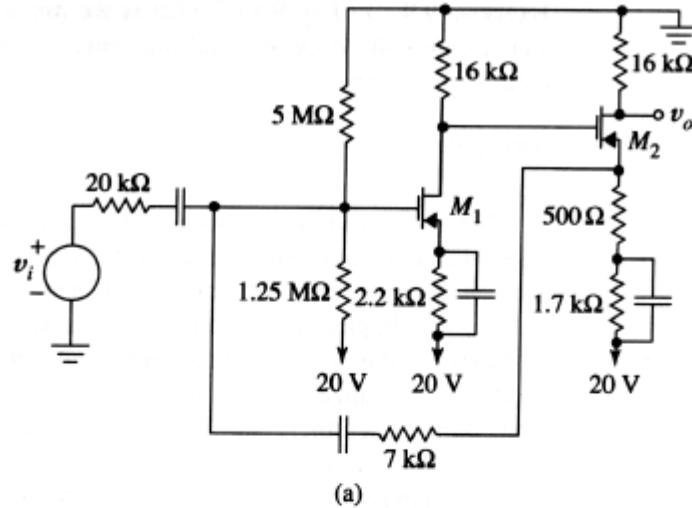


Connections for feedback in single-ended amplifiers: (a) voltage feedback; (b) current feedback; (c) shunt feedback; (d) series feedback.



Examples of single-ended feedback structures: (a) voltage shunt; (b) current shunt; (c) voltage series; (d) current series.

實例



FET current-shunt feedback amplifier: (a) circuit schematic; (b) feedback network and two-port equivalent; (c) midrange circuit for applying feedback theory.

其他注意事項：

- (1) R_{if} 與 R_{of} 的頻率響應
- (2) 穩定度：*Nyquist stability criterion*

放大器不穩定的充要條件為存在一頻率 ω_o ，其迴路增益

$$L(\omega_o) = A(\omega_o)\mathbf{b} = M\angle 180^\circ, \quad \text{and } M \geq 1$$