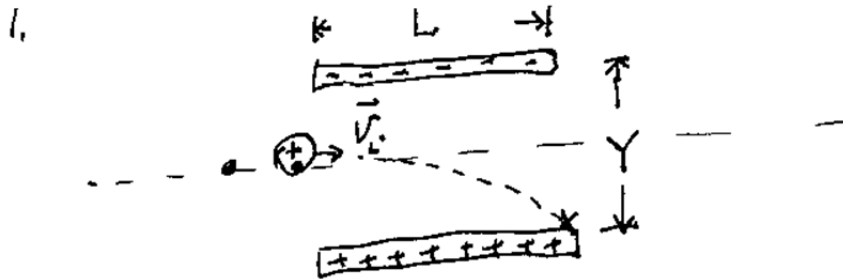




St. ID: \_\_\_\_\_

Name: \_\_\_\_\_

## Final Exam.2 -Solution



$$F_e = QE = ma \rightarrow \text{So the } a_y = \frac{-QE}{m}$$

$$v_x = v_i = \text{constant}$$

$$v_y = a_y t = -\frac{eE}{m} t$$

To hit the lower end, it has to be a negative charge, and travels  $\frac{1}{2} Y$  distance in the  $-y$  direction

$$\therefore \frac{1}{2} Y = \frac{1}{2} a_y t^2 = -\frac{1}{2} \frac{QE}{m} t^2$$

to get  $t$ , it is the distance and time in the  $\hat{x}$ -direction

$$x = v_i t, \quad t = \frac{L}{v_i}$$

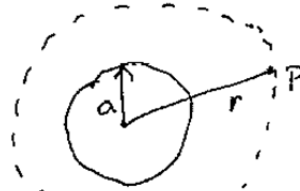
$$\therefore \frac{1}{2} Y = -\frac{1}{2} \frac{QE}{m} \left(\frac{L}{v_i}\right)^2$$

$$\therefore E = Y \frac{v_i^2}{L^2} \frac{m}{Q}$$

② A Spherically symmetric Charge distribution

②-1: A point outside the sphere

Pick a Gaussian surface bigger than the surface



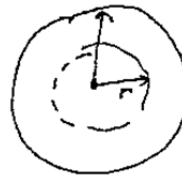
$$\Phi_E = \oint E \cdot dA = E \oint dA = E \cdot 4\pi r^2 = \frac{q}{\epsilon_0}$$

$$E = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} = k_e \frac{q}{r^2} \quad (r > a)$$

②-2. A point inside the sphere.

Pick a Gaussian surface as shown

$$q_{in} = \rho V = \rho \cdot \frac{4}{3} \pi r^3$$

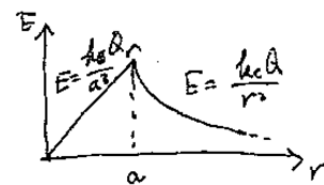


$$\Phi_E = \oint E dA = E \oint dA = E (4\pi r^2) = \frac{q_{in}}{\epsilon_0}$$

$$E = \frac{q_{in}}{4\pi\epsilon_0 r^2} = \frac{\rho (\frac{4}{3} \pi r^3)}{4\pi\epsilon_0 r^2} = \frac{\rho}{3\epsilon_0} r$$

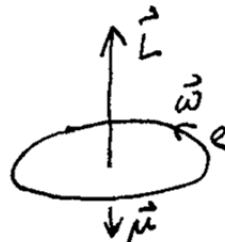
$$\rho = \frac{Q}{\frac{4}{3} \pi a^3}$$

$$\therefore E = \frac{Qr}{4\pi\epsilon_0 a^3} = k_e \frac{Q}{a^3} r \quad (r < a)$$



3

Consider an electron moving around the atom



$$I = \frac{Q}{T} = \frac{Q\omega}{2\pi} = \frac{Qv}{2\pi r} \quad , v = \text{linear velocity}$$

$$\mu = \cancel{IA} = IA = \frac{Qv}{2\pi r} \cdot \pi r^2 = \frac{1}{2} Qvr$$

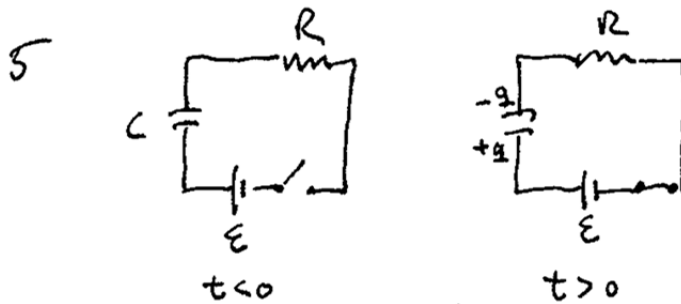
$$Qr, \quad \mu = \frac{1}{2m} mvrQ$$

$$\text{But } L = mvr$$

$$= \left(\frac{Q}{2m}\right) L = \left(\frac{Q}{2m}\right) L \quad \text{— This is the classical magnetic moment}$$

4. Let  $d$  is the diameter of the aperture, then  $d \sin \theta = \lambda$  is the first minimum of the central bright diffraction pattern.  $\theta = 1^\circ$ ,  $\sin \theta \cong \theta = 1^\circ = \pi/180$

$$\text{So, } d = \frac{420 \times 10^{-9} \text{ m}}{\sin(\frac{\pi}{180})} = \frac{420 \times 10^{-9}}{3.14/180} = 24 \mu\text{m}$$



Use Kirchhoff's law

$$\mathcal{E} - \frac{q}{C} - IR = 0$$

- ① at  $t=0$ , capacitor is not charged  $I_0 = \frac{\mathcal{E}}{R}$   
 When the capacitor is completely charged,  $I=0$

$$\mathcal{E} - \frac{q}{C} - IR = 0$$

$$Q = CV$$

$$I = \frac{\mathcal{E}}{R} - \frac{q}{RC}$$

$$\boxed{\frac{dq(t)}{dt} + \frac{1}{RC} q(t) - \frac{\mathcal{E}}{R} = 0} \quad \text{— Ans}$$

This is the first order differential equation

A possible solution is

$$q(t) = C\mathcal{E} (1 - e^{-t/RC})$$

$$= Q (1 - e^{-\frac{t}{RC}})$$

## 6. displacement current:

Maxwell introduced an extra term in Ampere's law to take care of the current induced ~~in~~ <sup>due to</sup> a time varying electric field.

$$\text{Ampere's law } \oint \mathbf{B} \cdot d\mathbf{s} = \mu_0 I$$

$$\text{Maxwell's } ~~law~~ \text{ equation } \oint \mathbf{B} \cdot d\mathbf{s} = \mu_0 (I + I_d)$$

$$I_d = \text{displacement current} \equiv \epsilon_0 \frac{d\Phi_E}{dt}$$