



St. ID: _____

Name: _____

Solutions:

- (a) Write down the first law of thermodynamics (Equation). [10+20 = 30]

Solution:

- $dE_{int} = dQ - dW$ (If the work is done by system)
or $dE_{int} = dQ + dW$ (If the work is done on the system by external source)

Where, E_{int} = Internal energy of a system
 Q = Heat
 W = Total work

- Mark (\checkmark) the right condition for the thermodynamical processes bellow:

Adiabatic process	$\checkmark Q = 0 / W = 0 / \Delta E_{int} = 0 ?$
Constant Volume process	$Q = 0 / \checkmark W = 0 / \Delta E_{int} = 0 ?$
Closed Cycle process	$Q = 0 / W = 0 / \checkmark \Delta E_{int} = 0 ?$
Free Expansion process	$\checkmark Q = W = 0 / \Delta E_{int} = 0 ?$

- For an isobaric expansion of an ideal gas at 300 K and 5.50 kPa, if the volume is increased from 1 m³ to 5 m³ and 12.5 kJ energy is transferred to the gas by heat. Find out (a) the change in its internal energy and (b) its final temperature ? [30]

Solution:

- We use the energy version of the non-isolated system model.

$$\Delta E_{int} = Q + W$$

Where, $W = -P\Delta V$ for a constant-pressure process so that

$$\begin{aligned} \Delta E_{int} &= Q - P\Delta V \\ &= 12.5 \text{ kJ} - 5.50 \text{ k Pa} (5 \text{ m}^3 - 1 \text{ m}^3) = 28 \text{ kJ} \end{aligned}$$

- Since pressure and quantity of gas are constant, we know the equation of state is

$$\frac{V_1}{T_1} = \frac{V_2}{T_2}$$

$$T_2 = \frac{V_2}{V_1} T_1 = \left(\frac{5 \text{ m}^3}{1 \text{ m}^3} \right) (300 \text{ K}) = 1500 \text{ K}$$

3. (a) Write down the formula of total kinetic energy of an ideal gas in terms of temperature (T). (b) If a 10-L of oxygen-cylinder contains O₂ gas at 22.0°C and 5 atm., find out the total translational kinetic energy of the gas molecules. (1 atm = 1.013×10⁵ Pa) [10+30 = 40]

Solution :

(a) Total kinetic energy, $K_{total} = \frac{3}{2} nRT$

Where , $n = N/N_A$ for the number of moles of gas

R= Universal gas constant (8.31 J/mol. K)

T = temperature

- (b) From the ideal gas law,

$$PV = nRT = \frac{2N}{3} \left(\frac{1}{2} m_0 v^2 \right) = \frac{N}{3} (m_0 v^2)$$

The total translational kinetic energy is $E_{trans} = N \left(\frac{1}{2} m_0 v^2 \right)$

$$E_{trans} = \frac{3}{2} PV = \frac{3}{2} (5 \times 1.013 \times 10^5 \text{ Pa}) (10 \times 10^{-3} \text{ m}^3)$$

$$\therefore E_{trans} = 7.59 \text{ kJ}$$