

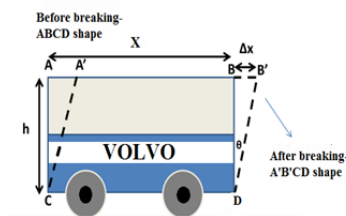
St. ID: _____,

Name: _____

Chapter: 12-15, Serway; ABSOLUTELY NO CHEATING!

Please write down the answers on the blank space or on the back of this paper. Answer should be in english. [] indicates the question points.

Q1. VOLVO is designing new generation Truck with automatic emergency breaking system using AI (Artificial Intelligence) to avoid unexpected accident. Suppose a VOLVO truck starts journey from Taipei to Hualien with a speed 100 km/hr and for a emergency breaking if the upper part of the truck is tilted $\Delta x = 50$ cm as shown in figure with respect to the base, what will be the “Shear Stress”, Shear Strain” and “Shear Modulus” for the deformation? Let the length of the truck $L= 15$ m, height, $h = 5$ m and during the break there has been 500 N force produced in the horizontal direction. [30 %]



Solution:

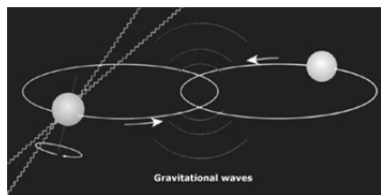
The total area of the truck body? $\sigma = (20 \times 5) \text{ m}^2 = 100 \text{ m}^2$,
 $F = 500 \text{ N}$ which is applied to the area, σ

We know, Shear stress = $\frac{\text{Applied Force}}{\text{Area}} = \frac{F}{\sigma} = \frac{500}{100} = 10 \text{ N/m}^2$

Shear strain = $\Delta x/h = 0.5/5 = 0.1$

Shear Modulus, $K = \frac{\text{Shear stress}}{\text{Shear strain}} = \frac{10 \text{ N/m}^2}{0.1} = 100 \text{ N/m}^2$

Q2. The gravitation wave is produced when two star systems merge/collide each other. If the two star systems of mass $M_1 = 2 \times 10^{50} \text{ kg}$ and $M_2 = 3 \times 10^{50} \text{ kg}$ are orbiting in their own orbitals as shown in figure below and if they experience $6 \times 10^{25} \text{ N}$ force during the generation of gravitational wave, Find out the separation distance between them? [30%]



Solution:

The gravitational force is defined by

$$F = G \frac{M_1 M_2}{r^2}, \text{ where } G \text{ is gravitational constant} = 6.674 \times 10^{-11} \text{ m}^3 \cdot \text{kg}^{-1} \cdot \text{s}^{-2}$$

we can write the separation distance,

$$r = \sqrt{G \frac{M_1 M_2}{F}} = \sqrt{6.674 \times 10^{-11} \text{ m}^3 \cdot \text{kg}^{-1} \cdot \text{s}^{-2} \frac{2 \times 10^{50} \text{ kg} \times 3 \times 10^{50} \text{ kg}}{6 \times 10^{25} \text{ N}}}$$

Therefore, $r = 2.58 \times 10^8 \text{ m}$

Q3. (a) If the gravitational wave is in simple harmonic motion and expressed by

$$y(x, t) = 4 \cos\left(\frac{8\pi}{20}x + 60\pi t + \phi\right),$$
 find-out the (i) wavelength (ii) frequency (iii) period and (iv)

amplitude of the motion. (Let, 'x' and 't' are in kilometer and second) (b) (i) Write down the Bernoulli's equation. (ii) Give two practical applications of Bernoulli's principle. [20 +20 = 40%]

Solution:

(a) By comparing the the equation $y(x, t) = 4 \cos\left(\frac{8\pi}{20}x + 60\pi t + \phi\right)$

with the standard wave equation $y(x, t) = A \cos\left(\frac{2\pi}{\lambda}x + \omega t + \phi\right)$

We can write ,

i) $\frac{2\pi}{\lambda} = \frac{8\pi}{20}$, therefore , the wavelength $\lambda = 5km$

ii) $\omega = 60\pi$

$$\Rightarrow 2\pi f = 60\pi$$

Therefore, $f = 30Hz$

iii) Period , $T = \frac{1}{f} = \frac{1}{30Hz} = 3.3 \times 10^{-2} \text{ sec}$

iv) Amplitude, $A = 4 km$

(b)

i) $P + \frac{1}{2}\rho v^2 + \rho gy = \text{Constant}$

where , P = pressure , ρ = density, v = velocity and y = lifting hight of the fluid

ii) Bernoulli's principle is used in Aircraft lifting , Carbtorator of the petrol/ desel engine of Car / Bus etc.