SN ： $\qquad$ ，Name： $\qquad$
Note：You can use pencil or any pen in answering the problems．Dictionary，calculators and mathematics tables are allowed．Please hand in both solution and this problem sheet． Answer must be in English．ABSOLUTELY NO CHEATING！

## Problems（total 6 problems，100\％）

1．Moment of Inertia：（ $15 \%$ ）What is the moment of inertia of a solid sphere of mass $\mathbf{M}$ ， radius $\mathbf{R}$ rotating about any of its diameter？

2．Rotational Kinetic energy：（15\％）A particle of mass $M$ is rotating in the circle about a certain origin with radius R with an angular velocity $\omega$ ．If you take a snap shot at a certain time $t$ ，what is the rotational kinetic energy？

3．Conservation of linear momentum：（15\％）Suppose two particles（with masses $\mathbf{M}_{1}$ and $\mathbf{M}_{2}$ ，velocities $\mathbf{V}_{1}$ and $\mathbf{V}_{2}$ ， respectively）collide in a two dimensional frictionless floor． During this collision，use Newton＇s third law；derive what is conserved if no external forces exist．The conserved term is defined as linear momentum．

4．Circular Motion：（20\％）A small sphere of mass $m$ is attached to the end of a cord of length R and set into motion in a vertical circle about a fixed point O as
 illustrated in Figure on the right．（a）Determine the tangential acceleration of the sphere and the tension in the cord at any instant when the speed of the sphere is $v$ and the cord makes an angle $\theta$ with the vertical．（b）What is the tension when the sphere is on the top and at the bottom positions？
5．Lennard－Jones Potenetial：（ $15 \%$ ）The potential energy associated with the force between two neutral atoms in a molecule can be modeled by the Lennard－Jones potential as $U(x)=4 \varepsilon\left[\left(\frac{\sigma}{x}\right)^{12}-\left(\frac{\sigma}{x}\right)^{6}\right]$ ，where $\mathbf{x}$ is the separation of the atoms．（a）What is the most likely distance between the two atoms？（5\％）（b）Given $\sigma=0.263 \mathrm{~nm}$ ，and $\varepsilon=1.51 \times 10-{ }^{22} \mathrm{~J}$ are two typical constants in a molecule，what is the atom separation in a typical chemical bond？（5\％）

6．Two－body collision with a spring：（20\％）Using the figure on the right，A block of mass $m_{1}=1.6 \mathrm{~kg}$

b initially moving to the right with a speed of $4.00 \mathrm{~m} / \mathrm{s}$ on a frictionless，horizontal track collides with a light spring attached to a second block of mass $\mathrm{m}_{2}=2.10 \mathrm{~kg}$ initially moving to the left with a speed of $2.50 \mathrm{~m} / \mathrm{s}$ as shown in the figure（a）．The spring constant is $600 \mathrm{~N} / \mathrm{m}$ ．（a）Find the velocities of the two blocks after the collision．（b） Determine the velocity of block 2 during the collision，at the instant block 1 is moving to the right with a velocity of $3.00 \mathrm{~m} / \mathrm{s}$ as shown in figure（b）．

