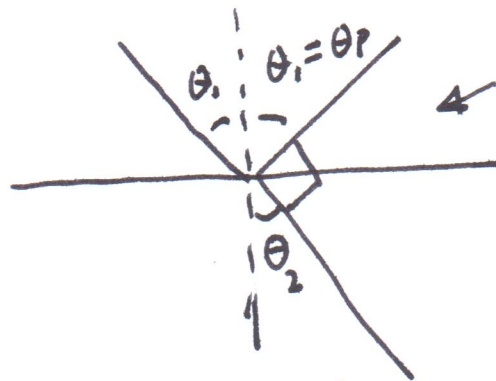


1. When the reflected and refracted light
 (a) is 90° , the reflection angle is $\theta_2 = \theta_p$
 θ_p is called Brewster angle

(b)



At this condition
 $\theta_2 = \theta_p \equiv$ Brewster angle

(c) From the above diagram

$$\theta_p + 90^\circ + \theta_2 = 180^\circ$$

Use Snell's law,

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

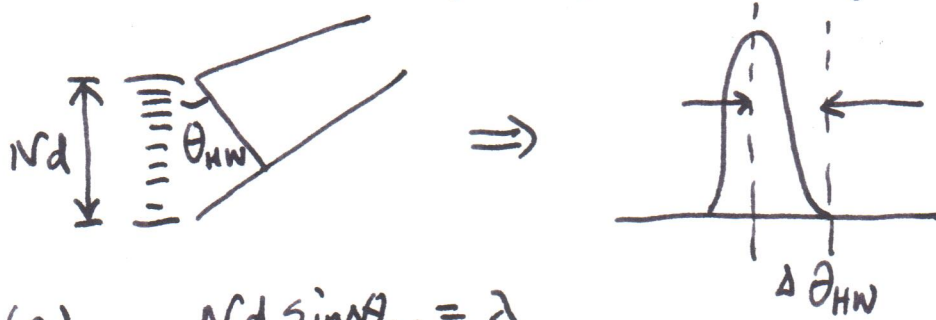
$$\frac{n_2}{n_1} = \frac{\sin \theta_1}{\sin \theta_2} = \frac{\sin \theta_p}{\sin (90^\circ - \theta_p)}$$

$$\therefore \tan \theta_p = \frac{n_2}{n_1}$$

(d) if $n_1 = \text{air} = 1$, then $\tan \theta_p = n_2$

This is the easiest way to find out
 the index of refraction of medium 2,

2. In a diffractive grating of ruling N , spacing d



(a) $Nd \sin \theta_{HW} = \lambda$

if $\Delta \theta_{HW}$ is small, $\sin \theta_{HW} = \Delta \theta_{HW}$

$\therefore \Delta \theta_{HW} = \frac{\lambda}{Nd}$

(b) ~~sin~~ $\sin \theta_{HW} = \frac{y}{D} = \frac{\lambda}{Nd} \Rightarrow y = D \frac{\lambda}{Nd}$

3

(a) For single slit diffraction, $a \sin \theta = \lambda$, for $m_1=1$ center bright

For double slit (Yang's), $d \sin \theta = m_2 \lambda$, for $m_2=0, 1, 2, \dots$

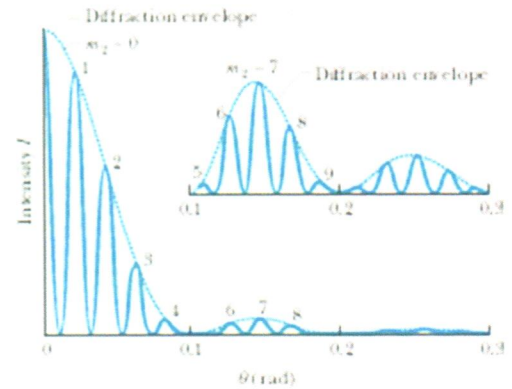
$$\text{Therefore, } m_2 = \frac{d}{a} = \frac{19.44 \mu\text{m}}{4.050 \mu\text{m}} = 4.8$$

For the center bright, there are 9 interference fringes

(b) At the second diffraction minimum, $a \sin \theta = 2\lambda$

$$m_2 = \frac{2d}{a} = \frac{(2)(19.44 \mu\text{m})}{4.050 \mu\text{m}} = 9.6$$

As shown in the right figure, there are only 4 bright interference fringes in either side band. There are total 8 bright fringes on the first side bands on both sides.



4.

a) The input voltage is $\Delta V_{\text{in}} = IZ = I\sqrt{R^2 + X_C^2} = I\sqrt{R^2 + (1/\omega C)^2}$. The output voltage is

$$\Delta V_{\text{out}} = IX_C = \frac{I}{\omega C}. \text{ The gain ratio is}$$

$$\frac{\Delta V_{\text{out}}}{\Delta V_{\text{in}}} = \frac{I/\omega C}{I\sqrt{R^2 + (1/\omega C)^2}} = \frac{1/\omega C}{\sqrt{R^2 + (1/\omega C)^2}}.$$

(b, c) As $\omega \rightarrow 0$, $\frac{1}{\omega C} \rightarrow \infty$ and R becomes negligible in comparison. Then

$$\frac{\Delta V_{\text{out}}}{\Delta V_{\text{in}}} \rightarrow \frac{1/\omega C}{1/\omega C} = \boxed{1}. \text{ As } \omega \rightarrow \infty, \frac{1}{\omega C} \rightarrow 0 \text{ and } \frac{\Delta V_{\text{out}}}{\Delta V_{\text{in}}} \rightarrow \boxed{0}.$$

$$(d) \frac{1}{2} = \frac{1/\omega C}{\sqrt{R^2 + (1/\omega C)^2}} \quad R^2 + \left(\frac{1}{\omega C}\right)^2 = \frac{4}{\omega^2 C^2} \quad R^2 \omega^2 C^2 = 3 \quad \omega = 2\pi f = \frac{\sqrt{3}}{RC}$$

$$\boxed{f = \frac{\sqrt{3}}{2\pi RC}}$$

5. In an AC circuit $\Delta V = \Delta V_{\max} \sin \omega t$

$$i = \frac{\Delta V}{R} = \frac{\Delta V_{\max} \sin \omega t}{R} = I_{\max} \sin \omega t$$

$$i_{\text{rms}} = \sqrt{\overline{i^2}}$$

$$i^2 = I_{\max}^2 \sin^2 \omega t$$

$$\therefore \overline{i^2} = \frac{1}{2} I_{\max}^2$$

$$\overline{i^2} = \frac{1}{T} \int I_{\max}^2 \sin^2 \omega t \, dt$$

$$= I_{\max}^2 \frac{1}{T} \int_0^T \sin^2 \omega t \, dt$$

$$i_{\text{rms}} = \sqrt{\overline{i^2}} = \frac{1}{\sqrt{2}} I_{\max}$$

$$= I_{\max}^2 \frac{1}{T} \int_0^T \left[\frac{1 - \sin\left(\frac{\omega t}{2}\right)}{2} \right] dt$$

$$P_{\text{AV}} = I_{\text{rms}}^2 R$$

$$= \frac{1}{2}$$

$$= \frac{1}{2} I_{\max}^2 R$$