Midterm

* <b>Note:</b> No points will be given if no arguments are provided for an answer.
• $\frac{d}{dx}[f(x)g(x)] = f'(x)g(x) + g'(x)f(x)$
• $\frac{d}{dx}\left(\frac{f(x)}{g(x)}\right) = \frac{g(x)f'(x) - f(x)g'(x)}{[g(x)]^2}$
• $\frac{d}{dx}f(g(x)) = f'(g(x))g'(x)$ and $\frac{d}{dx}x^r = rx^{r-1}$ , for all $r$
• $\frac{d}{dx}\sin(x) = \cos(x), \ \frac{d}{dx}\cos(x) = -\sin(x),$
• $\sin^2 x + \cos^2 x = 1$ , $\tan^2 x + 1 = \sec^2 x$
• $\tan(x) = \frac{\sin x}{\cos x}$ and $\sec x = \frac{1}{\cos x}$
Good Luck! $\sim \sim$ Yuling $\ddot{\sim}$

- 1. (8 points) Show that if a function f is differentiable at x = c, then it is continuous at x = c.
- 2. (8 points) Find the equation of the tangent line to the curve of  $2x + xy 2 = \ln(x^3 + y^2)$  at the point (1, 0).
- 3. (8 points) Find the equation of the tangent line to the graph of  $f(x) = x \ln(\sqrt{x})$  at the point where x = 1.
- 4. (16 points) Find the absolute maximum and absolute minimum (if any) of

(a) 
$$f(x) = \ln(4x - x^2)$$
 for  $1 \le x \le 3$ .

- (b)  $h(t) = (e^{-t} + e^t)^3$  for  $-1 \le t \le 3$ .
- 5. (40 points) Find the derivative  $\frac{dy}{dx}$  or f'(x) where
  - (a)  $f(x) = 6 \tan^3(\ln(\sqrt{3x}))$  (b)  $f(x) = x^x 6^{x^3}$
  - (c)  $f(x) = \arcsin(x) = \sin^{-1}(x)$ : the inverse function of  $\sin(x)$

(d) 
$$e^{2x-x^3}\log_5 y = 2y\sin(x^2) + y\ln((3x^2+1)^2)$$
 (e)  $y = \frac{(4x^3e^{-2x})^4(2x^5-8x+2)^3}{[1+\cos(5x^2-10x)+x^{5.2}]^{7.4}}$ 

- 6. (8 points) Find the second derivative, that is f''(x), of  $f(x) = e^{x^2-1} + 5e^{6x} + \ln(x^2+2)$ .
- 7. (24 points) Find the indicated limit or show it does not exist. If the limiting value is infinite, indicate whether it is  $\infty$  or  $-\infty$ .

(a) 
$$\lim_{x \to 0} (e^{-3x} + 5x)^{1/x}$$
 (b)  $\lim_{x \to 0} \frac{\sin(\sqrt{5x})}{\sin(3x)}$ , (c)  $\lim_{t \to \infty} t^3 e^{-5t}$ 

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