

\* Answer and mark clearly the questions in the provided answer sheets.  
Write down your name and student's ID on the each answer sheet you used.  
\* **Note:** No points will be given if no arguments are provided for an answer.  
*Good Luck!*                                      *~~ Yuling* ☺

1. (10 points) Find the domain and range of the function  $f(x) = \sqrt{1-x}$ .
2. (50 points) Find the indicated limit, if it exists. If the limiting value is infinite, indicate whether it is  $\infty$  or  $-\infty$ .

$$(a) \lim_{x \rightarrow 0} \frac{x^2 - x}{2x} \quad (b) \lim_{x \rightarrow 1} \frac{\sqrt{x} - 1}{x - 1} \quad (c) \lim_{x \rightarrow 1} \frac{2x - 2}{x^3 + x^2 - 2x}$$

$$(d) \lim_{x \rightarrow \infty} \frac{x^5 - x^3 + x - 1}{x^6 + 2x^2 + 1} \quad (e) \lim_{x \rightarrow 0^+} \frac{1}{x}$$

3. (10 points) Determine all values of  $x$  at which the function  $f$  is discontinuous, where

$$f(x) = \frac{x^2 - 2x}{x^2 - 3x + 2}.$$

4. (10 points) Let

$$f(x) = \begin{cases} x + 2 & \text{if } x \leq 1 \\ kx^2 & \text{if } x > 1 \end{cases}$$

Find the constants  $k$  that will make  $f$  continuous on  $(-\infty, \infty)$ .

5. (10 points) Show that the function  $f(x) = x^3 - 2x^2 + 3x + 2$  is continuous on the interval  $[-1, 1]$ , hence  $f$  must have at least one zero in the interval  $(-1, 1)$ .
6. (10 points) Let  $f(x) = 2x^2 + 1$ . Find the derivative  $f'$  of  $f$ , then find an equation of the tangent line to the curve at the point  $(1, 3)$ .