

## Notes

- Midterm will be held in class 0900-1100, 020425 (Thr). You can bring along a calculator and a cheatsheet of size A4 with you. I will explain this part in class. **Be Prepared!**
  - This midterm will cover (refer to **Content** of the Text): Ch 1 (except §1.5) , §2.1, §2.2, §3.2 (skip Example 3{8, Example 12), §3.3 (skip *Vector Space of Functions*, p151-154).
1. Let  $A$  be a  $m \times n$  matrix. Null space  $N(A)$  and Span (space).  $\exists (\mathbf{v}_1, \dots, \mathbf{v}_n)$  where  $\mathbf{v}_1, \dots, \mathbf{v}_n$  are vectors in  $V = R^m$ .
  2. Spanning set of  $V$
  3. Coordinate system of  $R^n$ . (Sets of vectors are) Linear independent and linearly dependent. Their connection with consistency of a linear system (Theorem)

## Homework

1. Do the Chapter test in the end of each chapter. They are very helpful.
2. §3.3: 2, 5, (contrasted with §3.2:12), 14, 16. Due 020425 in class before midterm.

## Reminder

### Determinant

You can calculate the determinant of a square matrix  $A$  by these rules

- If  $A$  is an elementary matrix of interchanging two rows (Type I, cf. p 68 in Text) then  $\det(A) = -1$
- If  $A$  is an upper triangular matrix with diagonal entries  $a_1, \dots, a_n$  then  $\det(A) = a_1 \cdots a_n$  (product of them).
- $\det(A) = \det(A^t)$ ;  $\det(\mathbf{B} A) = \det(A) \det(\mathbf{B})$ :

Consequently (you should be able to check them yourself),

- If  $A$  is an elementary matrix of Type II (multiplying a nonzero constant  $c$ , p 69), then  $\det(A) = c$
- If  $A$  is an elementary matrix of Type III (adding a multiple of one row to another, p 69), then  $\det(A) = 1$ :

### Nonsingularity of $A$ and consistency of $\mathbf{A}x = b$

Theorem 1.3.1 (p 42). Theorem 1.4.3 (p 71), Corollary 1.4.4 (p 72), Theorem 2.2.2 (p 110).  
Connection with linearly independency of column vectors of  $A$ . Theorem 3.3.1, Theorem 3.3.2.

